

TAMIBIA UNIVERSITY

OF SCIENCE AND TECHNOLOGY

FACULTY OF HEALTH, NATURAL RESOURCES AND APPLIED SCIENCES SCHOOL OF NATURAL AND APPLIED SCIENCES

DEPARTMENT OF MATHEMATICS, STATISTICS AND ACTUARIAL SCIENCE

QUALIFICATION: Bachelor of science; Bachelor of science in Applied Mathematics and Statistics				
QUALIFICATION CODE: 07BSAM	LEVEL: 6			
COURSE CODE: FIM601S	COURSE NAME: FINANCIAL MATHEMATICS 2			
SESSION: JULY 2023	PAPER: THEORY			
DURATION: 3 HOURS	MARKS: 100			

SECOND OPPORTUNITY EXAMINATION QUESTION PAPER				
EXAMINER	Dr V. Katoma			
,	Mrs. H.Y Nkalle			
MODERATOR:	Prof. A.S. Eegunjobi			

INSTRUCTIONS				
	•	Answer ALL the questions in the booklet provided.		
	•	Show clearly all the steps used in the calculations.		
	•	All written work must be done in blue or black ink and sketches		
		must be done in pencil.		

PERMISSIBLE MATERIALS

• Non-programmable calculator without a cover.

THIS QUESTION PAPER CONSISTS OF 3 PAGES (Including this front page)

Question 1 [25]

- 1.1 What is derivative? Mention two (2) purposes of derivatives. [3]
- **1.2** Mention four (4) elements under fixed interest government borrowings. [4]
- **1.3** Suppose a stock that pays no dividend is worth N\$60.00. The annual compounding interest rate is 5%. What is the one-year forward price of the stock? [4]
- 1.4 Consider a Put Option with a strike of N\$500.00.
 - (a) What would be the payoff to the buyer if the spot price at the expiration date is N\$ 550.00? [4]
 - (b) What would be the payoff to the buyer if the spot price at the expiration date is N\$ 450.00? [3]
- **1.5** Consider a 3×9 FRA for £2000.00 with an FRA rate of 5%. Suppose the reference rate is LIBOR and the 6-month LIBOR on the effective date is 6%. Assume ACT/360 and the loan is for a period of 120 days. Find how much the borrower receives from the lender on the effective date. [7]

Question 2 [25]

- **2.1** Consider the cash-flow sequences $e=(e_0,\ldots,e_n)$ and $m=(m_0,\ldots,m_n)$. When is the cashflow "e" preferable to "m"?
- **2.2** Consider the net cash flow sequences

A = (50, 51, -4), B = (50, 528, -22), at time t = 0, 1, 2. Suppose the net present value for **A** is 108 and that of **B** is 594 at time 2. Find the internal rate of return for each outlay. Suppose the interest of both cash flows is 7%, which one is a more viable investment?

[7]

2.3 VK Investment cc has an existing debt of N\$ 2000000 on which it makes annual payments at an annual effective rate of LIBOR plus 0.5%. VK Investment cc decides to enter a swap with a notional amount of N\$ 2000000 on which it makes annual payments at a fixed annual effective rate of 3% in exchange for receiving annual payments at the annual effective LIBOR rate. The annual effective LIBOR rates over the first and second years of the swap contract are 2.5% and 4% respectively. VK Investment cc does not make or receive any other payments. Calculate the net interest payment that VK Investment cc makes in the second year.

[10]

2.4 Explain the dangers of derivatives

[5]

Question 3 [25]

3.1 Suppose a certificate of deposit is issued with a face value of N\$ 500000.00 and a coupon of 6% for 90 days. After 30 days, its yield has fallen to 5.75%. What is the price?

[8]

- **3.2** Consider the cash flow sequence, a = (5, 9, 20, 4, 2), b = (6, 7, 3, 1, 36) at time t = 0, ..., 4. Find the Net Present Value (NPV) of the cash flow assuming an interest rate of 7%.
- **3.3** Suppose a loan size of l_0 is repaid by nm equal installments of size x at times
- $\frac{1}{m}, \frac{2}{m}, ..., \frac{nm}{m} = n$. Suppose the interest rate charged is i% per annum effective. Find an expression for the capital repayment for the k^{th} installment. [5]
- **3.4** Calculate the present value of an annuity of amount N\$ 100.00 paid annually for 5 years at the rate of interest of 9%. [5]

Question 4 [25]

- **4.1** An investment of N\$ 200.00 returns N\$ 120.00 at the end of 1st year and N\$ 100.00 at the end of 2nd year. What is the internal rate of return (IRR)? [5]
- **4.2** Explain the difference between a negotiable and non-negotiable financial instrument and give an example [3]
- **4.3** Frans is considering a project which requires an amount of N\$3000.00 and another amount of N\$1000.00 after one year. In two years', time, when the project ends, she expects an inflow of N\$4500.00. what is the internal rate of return (IRR) of this project? Is the above Investment profitable? Assume that Frans can lend and borrow at the same fixed rate of 7.13% per annum.
- **4.4** Consider the following two cash-flow sequences:

Time (Year)	0	1	2	3
Project A	-80	96	1	5
Project B	-80	10	10	90

Find the Internal Rate of Return (IRR) of project A and Project B. And show that IRR(A) > IRR(B). [8]

END of EXAM